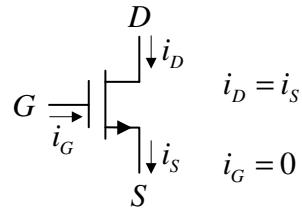


Režimi rada MOS tranzistora

➤ NMOS tranzistor



❖ Zasićenje:

$$v_{GS} > V_{TN} \text{ i } v_{GD} < V_{TN}$$

$$i_D = \frac{B}{2} (v_{GS} - V_{TN})^2 = \frac{\mu_n C_{ox} W}{2L} (v_{GS} - V_{TN})^2; \quad B = \frac{\mu_n C_{ox} W}{L}$$

❖ Triodna oblast:

$$v_{GS} > V_{TN} \text{ i } v_{GD} > V_{TN}$$

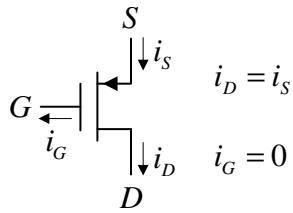
$$i_D = B \left[(v_{GS} - V_{TN}) v_{DS} - \frac{v_{DS}^2}{2} \right] = \frac{\mu_n C_{ox} W}{L} \left[(v_{GS} - V_{TN}) v_{DS} - \frac{v_{DS}^2}{2} \right]; \quad B = \frac{\mu_n C_{ox} W}{L}$$

❖ Zakočenje (OFF):

$$v_{GS} < V_{TN}$$

$$i_D = 0$$

➤ PMOS tranzistor



❖ Zasićenje:

$$v_{SG} > |V_{TP}| \text{ i } v_{DG} < |V_{TP}|$$

$$i_D = \frac{B}{2} (v_{SG} - |V_{TP}|)^2 = \frac{\mu_p C_{ox} W}{2L} (v_{SG} - |V_{TP}|)^2; \quad B = \frac{\mu_p C_{ox} W}{L}$$

❖ Triodna oblast:

$$v_{SG} > |V_{TP}| \text{ i } v_{DG} > |V_{TP}|$$

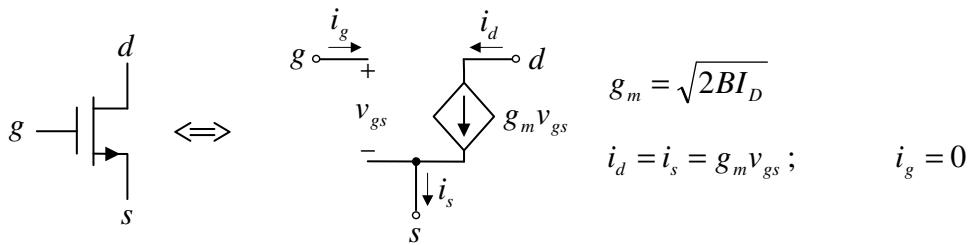
$$i_D = B \left[(v_{SG} - |V_{TP}|) v_{SD} - \frac{v_{SD}^2}{2} \right] = \frac{\mu_p C_{ox} W}{L} \left[(v_{SG} - |V_{TP}|) v_{SD} - \frac{v_{SD}^2}{2} \right]; \quad B = \frac{\mu_p C_{ox} W}{L}$$

❖ Zakočenje (OFF):

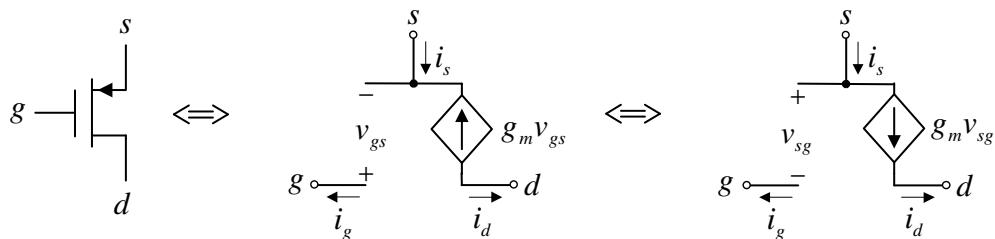
$$v_{SG} < |V_{TP}|$$

$$i_D = 0$$

➤ Model NMOS tranzistora za mali signal:



➤ Model PMOS tranzistora za mali signal:

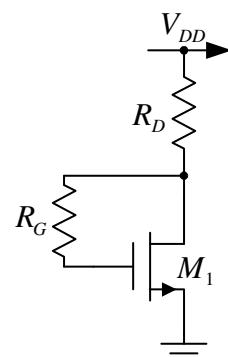


$$g_m = \sqrt{2BI_D}; \quad i_d = i_s = g_m v_{sg}; \quad i_g = 0$$

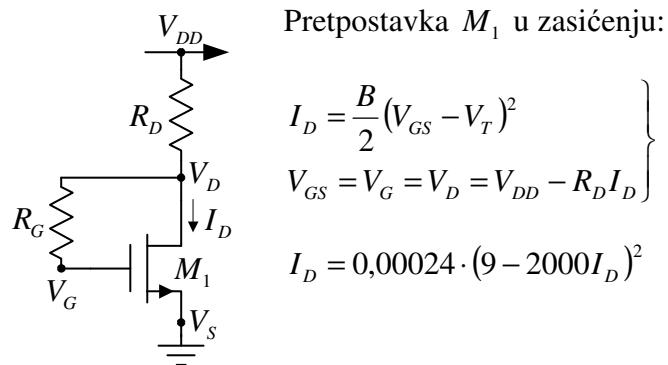
89. Parametri tranzistora u kolu sa slike su: $V_{TN} = V_T = 3V$ i

$$B = \frac{\mu_n C_{ox} W}{L} = 0,48 \text{ mA/V}^2, \text{ dok je } V_{DD} = 12V, R_D = 2k\Omega \text{ i } R_G = 10M\Omega.$$

Izračunati napone V_{GS} i V_{DS} .



Rešenje:



Prepostavka M_1 u zasićenju:

$$\left. \begin{aligned} I_D &= \frac{B}{2} (V_{GS} - V_T)^2 \\ V_{GS} &= V_G = V_D = V_{DD} - R_D I_D \end{aligned} \right\} \Rightarrow I_D = \frac{B}{2} (V_{DD} - R_D I_D - V_T)^2$$

$$I_D = 0,00024 \cdot (9 - 2000 I_D)^2$$

$$960I_D^2 - 9,64I_D + 0,01944 = 0$$

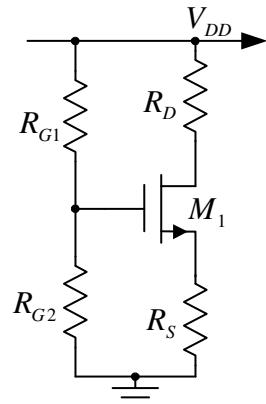
$I'_D = 7,25\text{mA} \Rightarrow V'_{GS} = V_{DD} - R_D I'_D = -2,5\text{V} < V_T \Rightarrow$ odbacuje se jer je M_1 po postavljenoj pretpostavci u zasićenju

$I''_D = 2,79\text{mA} \Rightarrow V''_{GS} = V_{DD} - R_D I''_D = 6,42\text{V} > V_T \Rightarrow$ prihvata se jer je u skladu sa postavljenom pretpostavkom da je M_1 u zasićenju

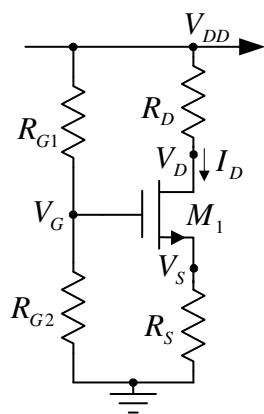
Dakle: $I_D = 2,79\text{mA}$, $V_{GS} = 6,42\text{V} > V_T$, $V_{GD} = 0 < V_T$, što znači da je M_1 zaista u zasićenju, tj. pretpostavka je tačna.

$V_{GS} = V_{DS} = 6,42\text{V}$

90. Parametri tranzistora u kolu sa slike su: $V_{TN} = V_T = 1\text{V}$ i $B = \frac{\mu_n C_{ox} W}{L} = 1\text{mA/V}^2$, dok je $V_{DD} = 10\text{V}$, $R_{G1} = R_{G2} = 10\text{M}\Omega$ i $R_D = R_S = 6\text{k}\Omega$. Izračunati struju I_D , kao i napone V_G , V_D i V_S .



Rešenje:



Pretpostavka M_1 u zasićenju:

$$\left. \begin{aligned} I_D &= \frac{B}{2} (V_{GS} - V_T)^2 \\ V_{GS} &= V_G - V_S = \frac{R_{G2}}{R_{G1} + R_{G2}} V_{DD} - R_S I_D = \frac{V_{DD}}{2} - R_S I_D \end{aligned} \right\} \Rightarrow$$

$$I_D = \frac{B}{2} \left(\frac{V_{DD}}{2} - R_S I_D - V_T \right)^2 \Rightarrow I_D = 0,0005 \cdot (4 - 6000 I_D)^2$$

$$18000I_D^2 - 25I_D + 0,008 = 0$$

$I'_D = 0,889 \text{mA} \Rightarrow V'_{GS} = \frac{V_{DD}}{2} - R_S I'_D = -0,334 \text{V} < V_T \Rightarrow$ odbacuje se jer je M_1 po postavljenoj pretpostavci u zasićenju

$I''_D = 0,5 \text{mA} \Rightarrow V''_{GS} = \frac{V_{DD}}{2} - R_S I''_D = 2 \text{V} > V_T \Rightarrow$ prihvata se jer je u skladu sa postavljenom pretpostavkom da je M_1 u zasićenju

Dakle: $I_D = 0,5 \text{mA}$, $V_{GS} = 2 \text{V} > V_T$, $V_{GD} = V_G - V_D = \frac{R_{G2}}{R_{G1} + R_{G2}} V_{DD} - (V_{DD} - R_D I_D) = -2 \text{V} < V_T$, što znači da je M_1 zaista u zasićenju, tj. pretpostavka je tačna.

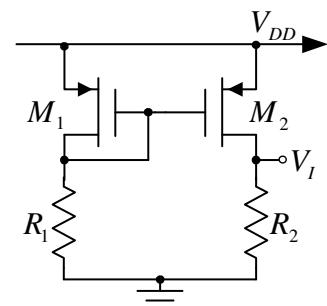
$$I_D = 0,5 \text{mA}$$

$$V_G = \frac{R_{G2}}{R_{G1} + R_{G2}} V_{DD} = \frac{V_{DD}}{2} \Rightarrow V_G = 5 \text{V}$$

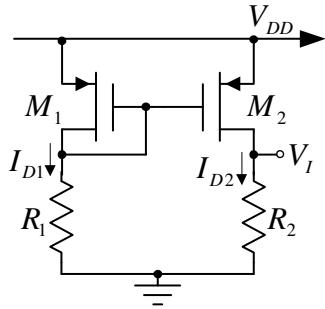
$$V_D = V_{DD} - R_D I_D \Rightarrow V_D = 7 \text{V}$$

$$V_S = R_S I_D \Rightarrow V_S = 3 \text{V}$$

91. Parametri tranzistora u kolu sa slike su: $V_{TP} = -V_T = -1 \text{V}$, $B_1 = \frac{\mu_p C_{ox} W_1}{L_1} = 2 \text{mA/V}^2$ i $B_2 = \frac{\mu_p C_{ox} W_2}{L_2} = 4 \text{mA/V}^2$, dok je $V_{DD} = 12 \text{V}$, $R_1 = 10 \text{k}\Omega$ i $R_2 = 4 \text{k}\Omega$. Izračunati struju drejna tranzistora M_1 , kao i napon V_I .



Rešenje:



Pretpostavka M_1 i M_2 u zasićenju:

$$\left. \begin{aligned} I_{D1} &= \frac{B_1}{2} (V_{SG1} - |V_{TP}|)^2 \\ V_{DD} - V_{SG1} - R_1 I_{D1} &= 0 \end{aligned} \right\} \Rightarrow V_{DD} - V_{SG1} - R_1 \frac{B_1}{2} (V_{SG1} - |V_{TP}|)^2 = 0$$

$$12 - V_{SG1} - 10(V_{SG1} - 1)^2 = 0$$

$$10V_{SG1}^2 - 19V_{SG1} - 2 = 0$$

$V'_{SG1} = -0,1V < |V_{TP}| \Rightarrow$ odbacuje se jer je M_1 po postavljenoj pretpostavci u zasićenju

$V''_{SG1} = 2V > |V_{TP}| \Rightarrow$ prihvata se jer je u skladu sa postavljenom pretpostavkom da je M_1 u zasićenju

$$V_{DD} - V_{SG1} - R_1 I_{D1} = 0 \Rightarrow I_{D1} = \frac{V_{DD} - V_{SG1}}{R_1} = 1\text{mA}$$

$$\left. \begin{aligned} I_{D1} &= \frac{B_1}{2} (V_{SG1} - |V_{TP}|)^2 \\ I_{D2} &= \frac{B_2}{2} (V_{SG2} - |V_{TP}|)^2 \\ V_{SG1} &= V_{SG2} \end{aligned} \right\} \Rightarrow \frac{I_{D1}}{I_{D2}} = \frac{B_1}{B_2} = \frac{1}{2} \Rightarrow I_{D2} = 2I_{D1} = 2\text{mA}$$

Dakle: $V_{SG1} = 2V > |V_{TP}|$, $V_{DG1} = 0 < |V_{TP}|$, što znači da je M_1 zaista u zasićenju; $V_{SG2} = V_{SG1} = 2V > |V_{TP}|$, $V_{DG2} = V_{D2} - V_{G2} = R_2 I_{D2} - (V_{DD} - V_{SG2}) = -2V < |V_{TP}|$, što znači da je M_2 zaista u zasićenju.

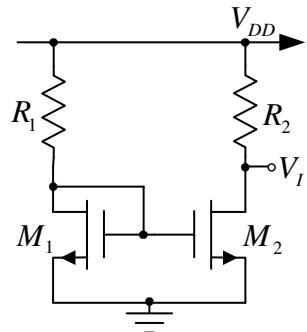
$$I_{D1} = 1\text{mA}$$

$$V_I = R_2 I_{D2} \Rightarrow V_I = 8\text{V}$$

92. (Zadatak za vežbu) Parametri tranzistora u kolu sa slike su:

$$V_{TN} = V_T = 1\text{V}, \quad B_1 = \frac{\mu_n C_{ox} W_1}{L_1} = 2\text{mA/V}^2 \quad i \quad B_2 = \frac{\mu_n C_{ox} W_2}{L_2} = 4\text{mA/V}^2,$$

dok je $V_{DD} = 12\text{V}$, $R_1 = 10\text{k}\Omega$ i $R_2 = 4\text{k}\Omega$. Izračunati struju drejna tranzistora M_1 , kao i napon V_I .



Rešenje:

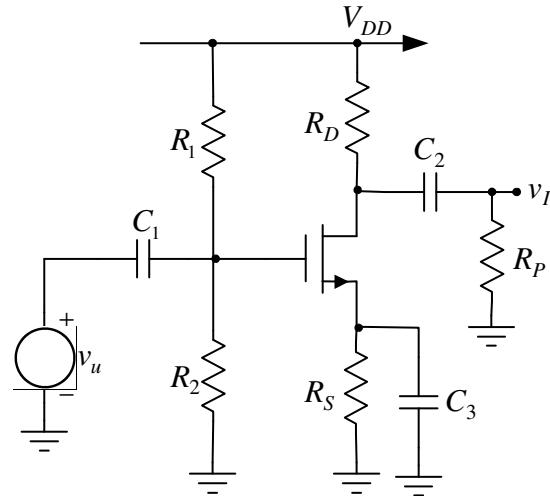
$$I_{D1} = 1\text{mA}$$

$$V_I = 4\text{V}$$

93. Za pojačavač sa slike je poznato: $V_{DD} = 12\text{V}$, $V_{TN} = V_T = 1\text{V}$, $B = \frac{\mu_n C_{ox} W}{L} = 0,5\text{mA/V}^2$, $C_1 \rightarrow \infty$, $C_2 \rightarrow \infty$, $C_3 \rightarrow \infty$, $R_1 = 20\text{k}\Omega$, $R_2 = 10\text{k}\Omega$, $R_D = 4\text{k}\Omega$, $R_S = 1\text{k}\Omega$ i $R_P = 4\text{k}\Omega$.

a) Izračunati jednosmernu struju drejna (I_D) i jednosmerne napone tranzistora (V_G , V_S i V_D).

b) Izračunati naponsko pojačanje pojačavača $a_v = \frac{v_i}{v_u}$, ulaznu otpornost koju vidi generator naizmeničnog signala v_u i izlaznu otpornost koju vidi potrošač R_P .

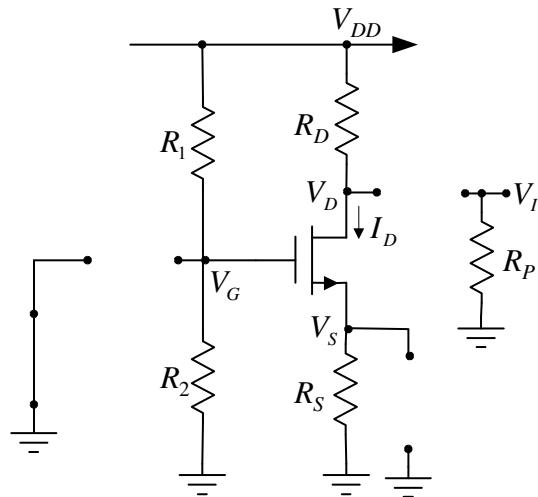


Rešenje:

a) DC analiza:

Formiranje šeme za DC analizu:

- ukidanje svih naizmeničnih generatora;
- zamena kondenzatora otvorenim vezama.



Tranzistor je u zasićenju (preduslov da bi pojačavač ispravno radio)!

$$\left. \begin{aligned} I_D &= \frac{B}{2} (V_{GS} - V_T)^2 \\ V_{GS} &= V_G - V_S = \frac{R_2}{R_1 + R_2} V_{DD} - R_S I_D = \frac{V_{DD}}{3} - R_S I_D \end{aligned} \right\} \Rightarrow$$

$$I_D = \frac{B}{2} \left(\frac{V_{DD}}{3} - R_S I_D - V_T \right)^2 \Rightarrow I_D = 0,00025 \cdot (3 - 1000 I_D)^2$$

$$10^6 \cdot I_D^2 - 10^4 \cdot I_D + 9 = 0$$

$$I'_D = 9 \text{ mA} \Rightarrow V'_{GS} = \frac{V_{DD}}{3} - R_S I'_D = -5 \text{ V} < V_T \Rightarrow \text{odbacuje se jer } M_1 \text{ mora biti u zasićenju}$$

$$I''_D = 1 \text{ mA} \Rightarrow V''_{GS} = \frac{V_{DD}}{3} - R_S I''_D = 3 \text{ V} > V_T \Rightarrow \text{prihvata se jer je u skladu sa činjenicom da } M_1 \text{ mora biti u zasićenju}$$

$$I_D = 1 \text{ mA}$$

$$V_G = \frac{R_2}{R_1 + R_2} V_{DD} = \frac{V_{DD}}{3} \Rightarrow \boxed{V_G = 4\text{V}}$$

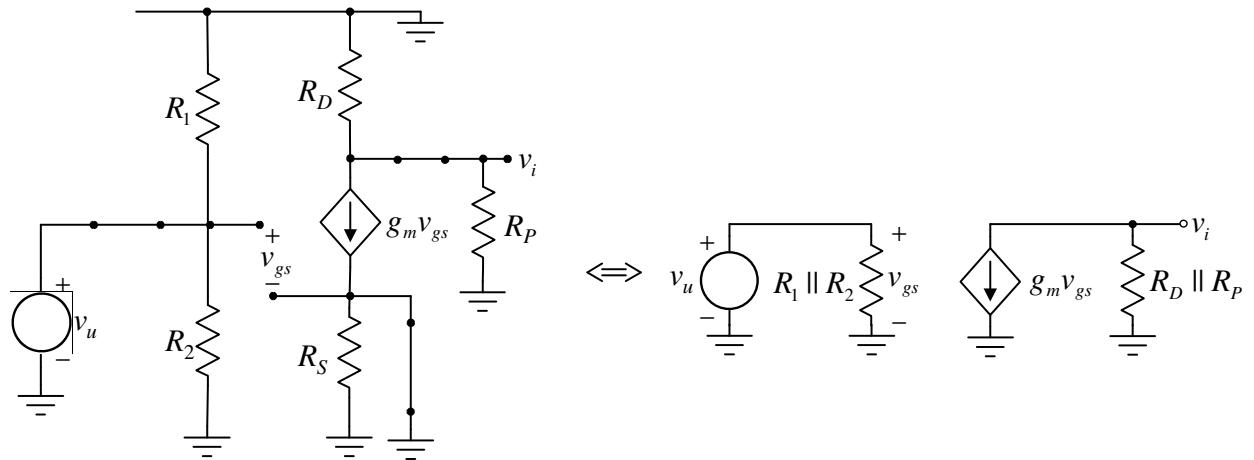
$$V_D = V_{DD} - R_D I_D \Rightarrow \boxed{V_D = 8\text{V}}$$

$$V_S = R_S I_D \Rightarrow \boxed{V_S = 1\text{V}}$$

b) AC analiza:

Formiranje šeme za AC analizu:

- ukidanje svih jednosmernih generatora;
- zamena kondenzatora $C \rightarrow \infty$ kratkim spojevima;
- zamena tranzistora modelom za mali signal.



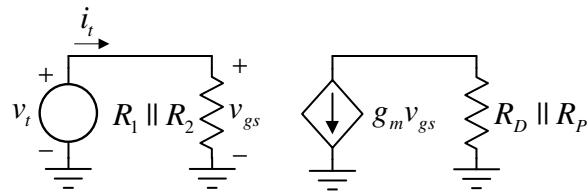
$$g_m = \sqrt{2BI_D} = 1\text{mS}$$

$$\left. \begin{aligned} v_i &= -g_m v_{gs} (R_D \parallel R_P) \\ v_{gs} &= v_u \end{aligned} \right\} \Rightarrow v_i = -g_m v_u (R_D \parallel R_P) \Rightarrow a_v = \frac{v_i}{v_u} = -g_m (R_D \parallel R_P) \Rightarrow$$

$$\boxed{a_v = -2}$$

Šema za računanje ulazne otpornosti:

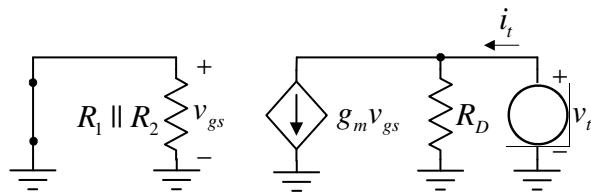
- povezivanje naponskog test generatora v_t između ulazne tačke i mase i označavanje struje i_t ;
- ukidanje svih nezavisnih generatora u ostatku kola;
- $R_{ul} = \frac{v_t}{i_t}$;



$$v_t = (R_1 \parallel R_2) i_t \Rightarrow R_{ul} = \frac{v_t}{i_t} = R_1 \parallel R_2 \Rightarrow [R_{ul} = 6,67 \text{k}\Omega]$$

Šema za računanje izlazne otpornosti:

- povezivanje naponskog test generatora v_t između izlazne tačke i mase i označavanje struje i_t ;
- ukidanje svih nezavisnih generatora u ostatku kola;
- $R_{izl} = \frac{v_t}{i_t}$;

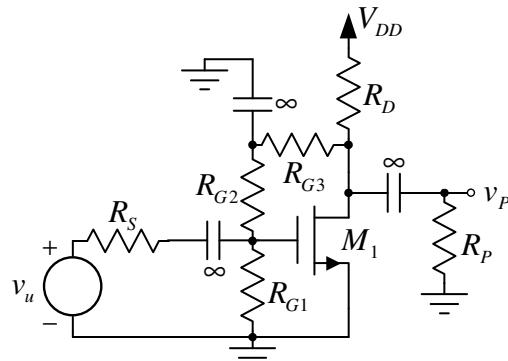


$$v_{gs} = 0 \Rightarrow g_m v_{gs} = 0 \Rightarrow v_t = R_D i_t \Rightarrow R_{izl} = \frac{v_t}{i_t} = R_D \Rightarrow [R_{izl} = 4 \text{k}\Omega]$$

94. Za pojačavač sa slike je poznato: $V_{DD} = 10V$, $V_{TN} = V_T = 1V$, $B = \frac{\mu_n C_{ox} W}{L} = 0,5 \text{mA/V}^2$, $R_{G1} = 2\text{M}\Omega$, $R_{G2} = 2\text{M}\Omega$, $R_{G3} = 1\text{M}\Omega$, $R_D = 20\text{k}\Omega$, $R_S = 10\text{k}\Omega$ i $R_P = 100\text{k}\Omega$.

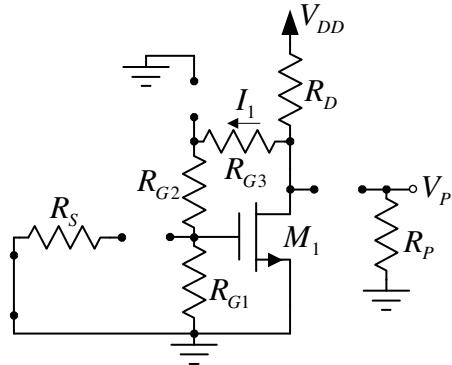
a) Izračunati jednosmernu struju drejna I_D i jednosmerne napone V_{GS} i V_{DS} .

b) Izračunati naponsko pojačanje pojačavača $a_v = \frac{v_p}{v_u}$, ulaznu otpornost koju vidi generator naizmeničnog signala v_u i izlaznu otpornost koju vidi potrošač R_P .



Rešenje:

a) DC analiza:



Tranzistor je u zasićenju (preduslov da bi pojačavač ispravno radio).

$$\left. \begin{aligned} V_{DS} &= V_{DD} - R_D(I_D + I_1) \\ I_1 &= \frac{V_{DS}}{R_{G3} + R_{G2} + R_{G1}} = \frac{V_{DS}}{5 \cdot 10^6} \\ I_D &= \frac{B}{2}(V_{GS} - V_T)^2 \\ V_{GS} &= \frac{R_{G1}}{R_{G3} + R_{G2} + R_{G1}} \cdot V_{DS} = 0,4V_{DS} \end{aligned} \right\} \Rightarrow V_{DS} = 10 - 2 \cdot 10^4 \cdot \left(2,5 \cdot 10^{-4} \cdot (0,4V_{DS} - 1)^2 + \frac{V_{DS}}{5 \cdot 10^6} \right)$$

$$0,8V_{DS}^2 - 2,996V_{DS} - 5 = 0$$

$V'_{DS} \approx 5\text{V} \Rightarrow V'_{GS} = 0,4V'_{DS} \approx 2\text{V} > V_T \Rightarrow$ prihvata se jer je u skladu sa činjenicom da M_1 mora biti u zasićenju

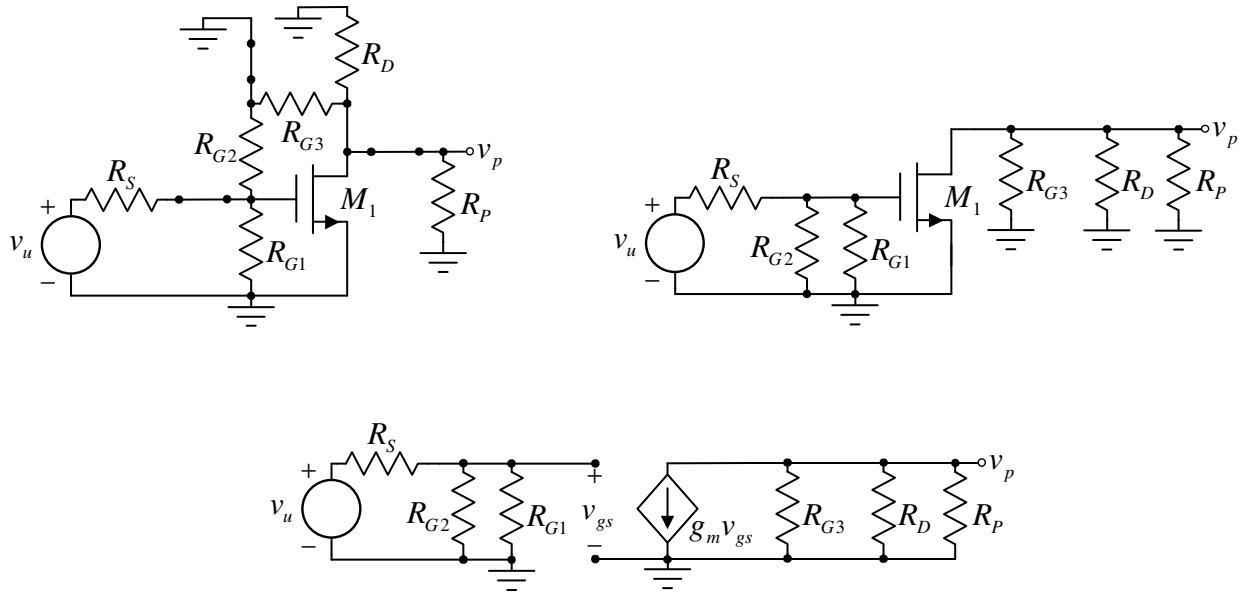
$V''_{DS} \approx -1,25\text{V} \Rightarrow V''_{GS} = 0,4V''_{DS} \approx -0,5\text{V} < V_T \Rightarrow$ odbacuje se jer M_1 mora biti u zasićenju

$$V_{DS} \approx 5\text{V}$$

$$V_{GS} \approx 2\text{V}$$

$$I_D = \frac{B}{2}(V_{GS} - V_T)^2 \Rightarrow I_D \approx 250\mu\text{A}$$

b) AC analiza:

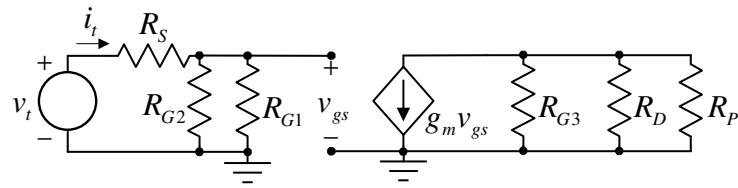


$$g_m = \sqrt{2BI_D} = 0,5\text{mS}$$

$$\left. \begin{aligned} v_p &= -g_m v_{gs} (R_D \parallel R_P \parallel R_{G3}) \\ v_{gs} &= \frac{R_{G1} \parallel R_{G2}}{R_s + R_{G1} \parallel R_{G2}} v_u \end{aligned} \right\} \Rightarrow v_p = -g_m \frac{R_{G1} \parallel R_{G2}}{R_s + R_{G1} \parallel R_{G2}} (R_D \parallel R_P \parallel R_{G3}) v_u \Rightarrow$$

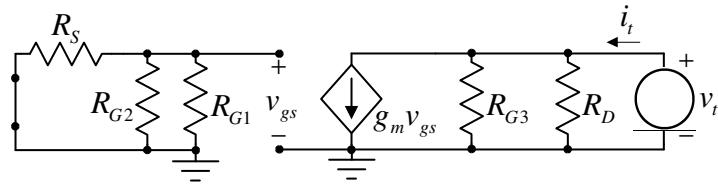
$$a_v = \frac{v_p}{v_u} = -g_m \frac{R_{G1} \parallel R_{G2}}{R_s + R_{G1} \parallel R_{G2}} (R_D \parallel R_P \parallel R_{G3}) \Rightarrow a_v = -8,116$$

Šema za računanje ulazne otpornosti:



$$v_t = (R_S + R_{G1} \parallel R_{G2}) i_t \Rightarrow R_{ul} = \frac{v_t}{i_t} = R_S + R_{G1} \parallel R_{G2} \Rightarrow \boxed{R_{ul} = 1,01 \text{ M}\Omega}$$

Šema za računanje otpornosti koju vidi potrošač:



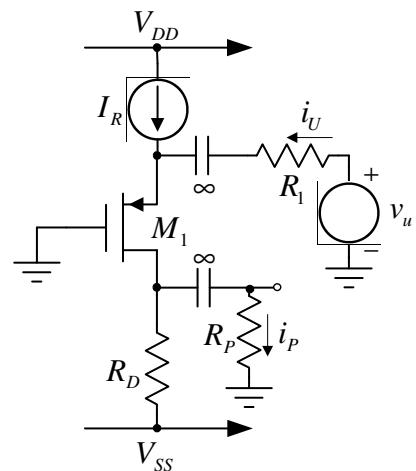
$$v_{gs} = 0 \Rightarrow g_m v_{gs} = 0 \Rightarrow v_t = (R_D \parallel R_{G3}) i_t \Rightarrow R_{izl} = \frac{v_t}{i_t} = R_D \parallel R_{G3} \Rightarrow \boxed{R_{izl} = 19,61 \text{ k}\Omega}$$

95. U pojačavaču sa slike parametri tranzistora su: $V_{TP} = -V_T = -1 \text{ V}$ i $B = 1 \text{ mA/V}^2$, dok je $V_{DD} = -V_{SS} = 10 \text{ V}$, $R_l = 250 \Omega$, $R_D = 2 \text{ k}\Omega$, $R_P = 6 \text{ k}\Omega$ i $I_R = 2 \text{ mA}$.

a) Odrediti jednosmerne vrednosti napona na drejnu i sorsu, kao i jednosmernu struju drejna tranzistora.

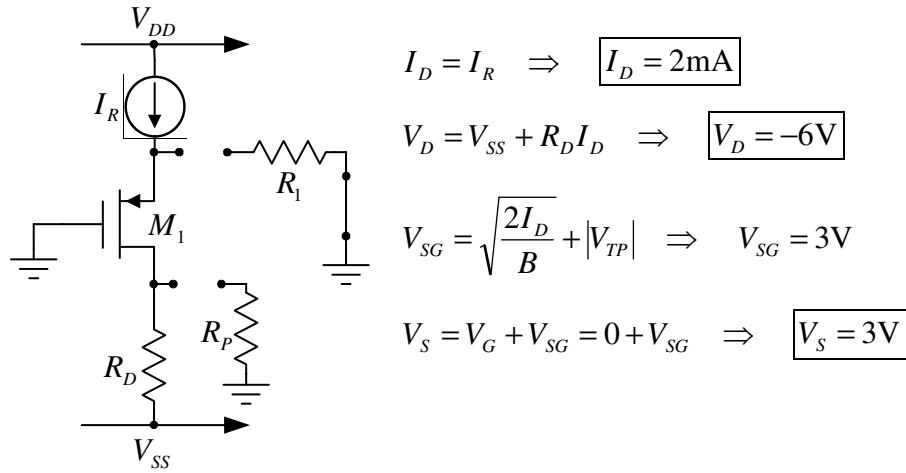
b) Odrediti strujno pojačanje pojačavača $a_i = i_p / i_u$.

c) Odrediti otpornosti koje vide ulazni generator i potrošač.

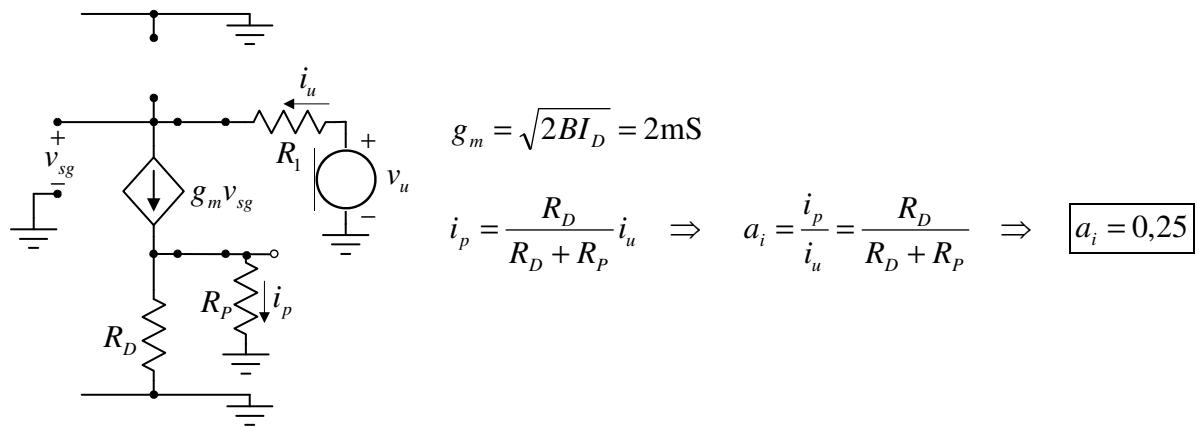


Rešenje:

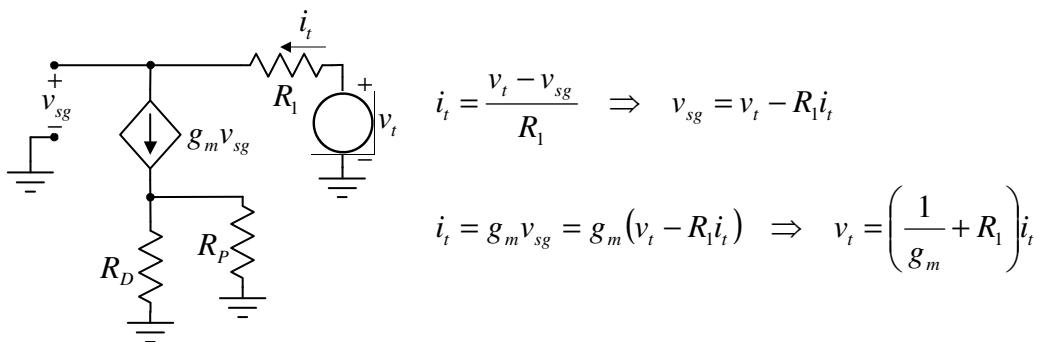
a) DC analiza:



b) AC analiza:

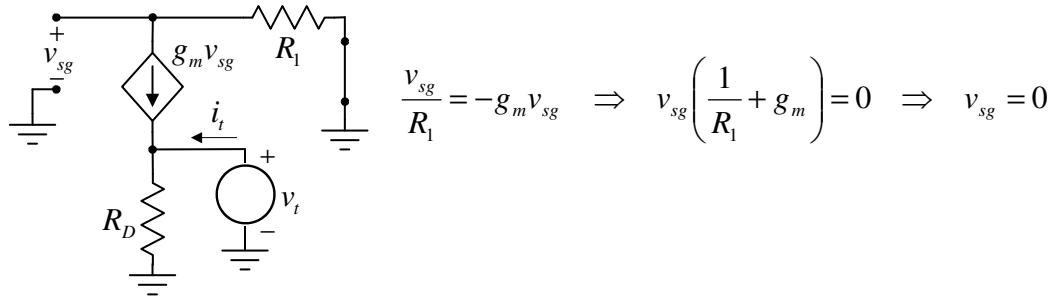


c) Šema za računanje ulazne otpornosti:



$$R_{ul} = \frac{v_t}{i_t} = \frac{1}{g_m} + R_l \Rightarrow \boxed{R_{ul} = 750\Omega}$$

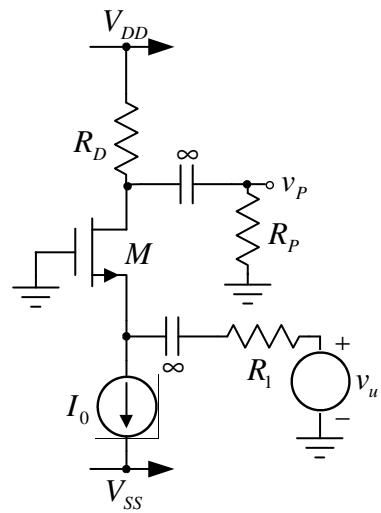
Šema za računanje otpornosti koju vidi potrošač:



$$v_{sg} = 0 \Rightarrow g_m v_{sg} = 0 \Rightarrow v_t = R_D i_t \Rightarrow R_{izl} = \frac{v_t}{i_t} = R_D \Rightarrow \boxed{R_{izl} = 2k\Omega}$$

96. (Zadatak za vežbu) U pojačavaču sa slike parametri tranzistora su: $B = 1 \text{ mA/V}^2$ i $V_T = 1 \text{ V}$, dok je: $V_{DD} = -V_{SS} = 10 \text{ V}$, $R_l = 250\Omega$, $R_D = 10 \text{ k}\Omega$, $R_P = 30 \text{ k}\Omega$ i $I_0 = 500 \mu\text{A}$.

- a) Odrediti jednosmerne vrednosti napona na sorsu i drejnu, kao i jednosmernu struju drejna.
- b) Odrediti naponsko pojačanje pojačavača $a = v_p / v_u$.
- c) Odrediti ulaznu otpornost i otpornost koju vidi potrošač R_P .



Rešenje:

a) $I_D = 500\mu A$

$V_D = 5V$

$V_S = -2V$

b) $a_v = \frac{v_p}{v_u} = \frac{g_m(R_D \parallel R_P)}{1 + g_m R_1} \Rightarrow a_v = 6$

c) $R_{ul} = R_1 + \frac{1}{g_m} \Rightarrow R_{ul} = 1,25k\Omega$

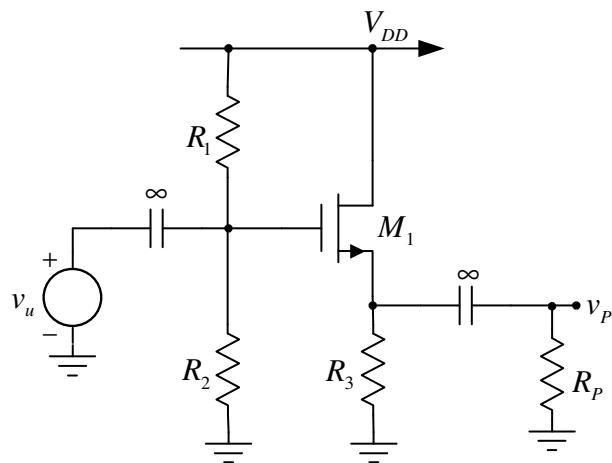
$R_{izl} = R_D \Rightarrow R_{izl} = 10k\Omega$

97. (Zadatak za vežbu) U pojačavaču sa slike, parametri tranzistora su: $V_T = 1V$, $B = \frac{\mu_n C_{ox} W}{L} = 1 \frac{mA}{V^2}$, dok je: $V_{DD} = 5V$, $R_1 = 128k\Omega$, $R_3 = 10k\Omega$ i $R_P = 20k\Omega$. Odrediti:

a) Otpornost R_2 tako da jednosmerni napon na sorsu bude $V_S = \frac{V_{DD}}{2}$;

b) Naponsko pojačanje pojačavača $a_v = \frac{v_p}{v_u}$;

c) Ulaznu otpornost i otpornost koju vidi potrošač.



Rešenje:

a) $R_2 = 680\text{k}\Omega$

b) $a_v = \frac{v_p}{v_u} = \frac{g_m(R_3 \parallel R_P)}{1 + g_m(R_3 \parallel R_P)} \Rightarrow a_v = 0,825$

c) $R_{ul} = R_1 \parallel R_2 \Rightarrow R_{ul} = 107,7\text{k}\Omega$

$R_{izl} = R_3 \parallel \frac{1}{g_m} \Rightarrow R_{izl} = 1,24\text{k}\Omega$

OSNOVI DIGITALNE ELEKTRONIKE (13S042ODE)

- Izborni predmet u na drugoj godini (u četvrtom semestru) Odseka za softversko inženjerstvo (6 kredita)
- Predavanja (2 časa nedeljno): dr Milan Ponjavić
- Računske vežbe (2 časa nedeljno): mr Goran Savić
- Detaljnije informacije i prezentacija predmeta na sajtu: <http://tnt.etf.rs/~si2ode>
